SHADOWS APPENDIX: MANUAL METHODS FOR CALCULATING SHADOWS

If access to the use of three-dimensional computer modeling software is not available, it is possible to graphically calculate the shadows for the Tier 3 Screening Analysis (Subsection 314) and the Detailed Shadow Analysis (Section 320), without the use of a computer. The methodologies outlined in this appendix can be used to carry out in a graphic form the shadow analyses described in Sections 314 and 320. All other analyses and assessments should be performed as outlined in the remaining sections of Chapter 8, "Shadows."

A. MANUAL METHOD FOR CALCULATING SHADOWS FOR THE TIER 3 SCREENING ANALYSIS

For an introduction to this part and related material regarding shadows analyses, see Subsection 314 (Tier 3 Screening Analysis).

The first step in the Tier 3 screening analysis is to determine the angle of the project's shadow on such sinlicutsensitive resource in relation to true north. On the base map (see Subsection 311), are valine from the project on the
building's footprint (or the corner of the project site, if the shape of the building is uning wn) that will cast the earliest
shadow on each open space or sun-sensitive architectural resource to the point on the open space or architectural resource that will first be in shadow. As explained in Section 100, above, because the sun rises in the cast and travels
across the southern part of the sky to set in the west, a project's earliest shadows would be cast almost directly westward. Throughout the day, they would shift clockwise (moving portlywork then north, they northeast) until sunset,
when they would fall east. Therefore, a project's earliest shadow of an open space or architectural resource would occur in this same pattern, depending on the location of the open space or resource in relation to the project site. A simple method to find the earliest shadow is to begin with a line norming due west somether project site. If this line does
not meet the open space or architectural resource, rotate the line clockwise until those. In the example in Figure A1,
the earliest shadow on an open space is represented by a line between the southeast corner of the project site and the
northwest corner of the open space. Intersect this line with a vertical line (a line drawn true north). This displays the
shadow's angle from true north when it enters the open space or reches the architectural resource. This is referred to
as the "entering angle" in this discussion.





FIGURE A1

Entering and Exiting Shadow Angles and Distances to Open Space



Using the same approach, draw a line from the point on the building's footprint that will cast the latest shadow on the open space or architectural resource to the point in the open space that will last be in shadow. In the example, this is the line between the northwest corner of the site and the southeast corner of the open space. Intersect this line with a vertical line (a line drawn true north) to display the shadow's angle from true north as it leaves the open space or resource. This is the "exiting angle."

All angles between the two angles obtained above represent the portions of the open space or resource that could be in the shadow of the proposed project at some time during the year. In this example, these angles, measured using a protractor, are -6 degrees (a minus sign means that the shadow occurs before approximately noon) and 57 degrees for the entering and exiting shadows, respectively.

The entering and exiting angles set the limits of shadows that the project would cast on the open space or resource at all times of the year. In this example, these angles, measured using a protractor, are or legices (minus sign many that the shadow occurs in the morning) and 57 degrees. This means that at any angle many or degrees to 57 degrees the building could potentially cast a shadow that would reach the open space.

Next, using Table A1, which gives the maximum shadow length factors for all shadow angles, detending the maximum shadow length of the building in question. The longest shadow that any building will cast along the year occurs on December 21st. The maximum shadow length for all angles between 66 and 50 degrees is 4.3 for 12 degrees on December 21st. This means that a 850-foot building, for example, would cast a haximum shadow of 1655 feet.

It may be necessary to adjust this calculation to account for differences in elevation between the building and the park or resource in question. If inspection of available maps shows, followample, that the building site is at an elevation approximately 20 feet higher than the park, that 20 feet is accled to the building height in making the calculation. This provides the building height relative to the elevation of the park. With the difference in elevation, the maximum shadow length that could occur would be 3741 feet (4.3 times 870), about 86 feet longer than the shadow for the building at the same elevation as the open space.

If the analysis above indicates or cannot calle out that shadows from the proposed project would reach a sunlight-sensitive resource at any time during the year, a detailed shadow analysis is required. The manual method for performing this detailed analysis is described in Part B. If the results of the screening analysis demonstrate that no shadows will reach any sunlight-sensitive resources, to further shadow assessment is needed. Provide the necessary documentation to support this conclusion illustrating the screening analysis.

As shown on Figure A2, the distances between the project site and the open space range from 404 to 802 feet. Therefore, a 850-foot building would cast a shad we acring the open space at some point in the year, and the next step in the screening is required.



FIGURE A2

Angles and Distances to Open Space





B. MANUAL METHOD FOR CALCULATING SHADOWS FOR THE DETAILED SHADOW ANALYSIS

For an introduction to this part and related material regarding shadows analyses, see Subsection 314.2 (Determining the "worst case" scenario for shadows), Subsection 314.3 (Months of interest and representative days for analysis), Subsection 314.4 (Timeframe window of analysis), Section 320 (Detailed Shadow Analysis), Subsection 321 (Future No-Action conditions), Subsection 322 (Future With-Action conditions), Subsection 324 (Performing the detailed analysis), and Subsection 325 (Documenting the extent and duration of incremental shadows).

The example presented in this section supposes an existing open space and a building that rises 640 feet without set-back and then slopes back to a pointed, dome-like, symmetrical top at 850 feet. Therefore, the positions on the ground from which to measure the length of the shadow (and distance to the open space) would be the three leading corners and the center of the site, labeled A, B, C, and D, respectively on Figure A2. As shown on this example, the shortest distance to the open space is a line drawn from B to E, which yields an angle of 52 degrees from true north are necessarily degrees from true north and measures 523 feet.

Having identified "worst case" shadow conditions (see *Subsection* 314.2), text onsult Table A2, when provides shadow length factors for all shadows angles for four representative days within the months of concern. Consider whether the entering and exiting angles and the angle defining the shorten district between the building and the open space or resource would cast shadows long enough to reach the open space or resource. Figures B1, B2, B3, and B4 illustrate the shadows that would occur from the 850-foot building example at an open space nearly. As shown in these figures, entering and/or exiting shadows would reach the park of December 21 and March 21. For May 6, the entering and exiting shadows would not reach the open space, but at the stortest point (52 legrees), the shadow angle factor would be 0.68, the length of the shadow would be 0.68 times 44% or 435 fact. This is more than the distance between the site and the park at that point; therefore, the shadow would enter at different and extend into the park.

In the example, on June 21, no shadow from the building would a tend into the open space. The entering and exiting shadows would not reach the open space. The shadow over the shortest distance from the site to the park (B to E) would be 0.46 times 640, or 294 feet (110 feet less than 404 feet). Over the shortest distance from the tallest point to the park (D to E) the shadow would be 0.40 times 850, or 340 feet. This is less than the distance between D and E on the ground (523 feet). Thus, no project shadow would enter the open space on June 21.





FIGURE **B1**

Shadows from 850-foot Building: June 21

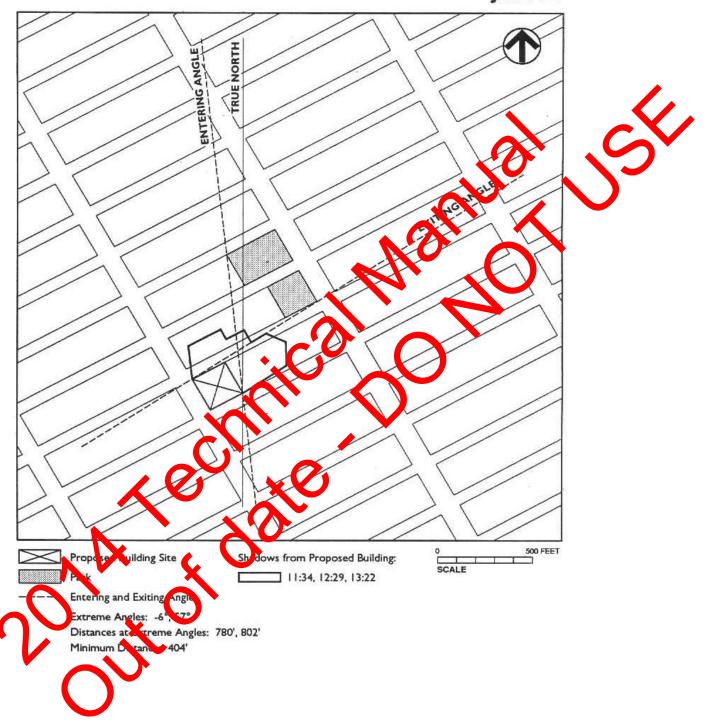




FIGURE B2

Shadows from 850-foot Building: May 6

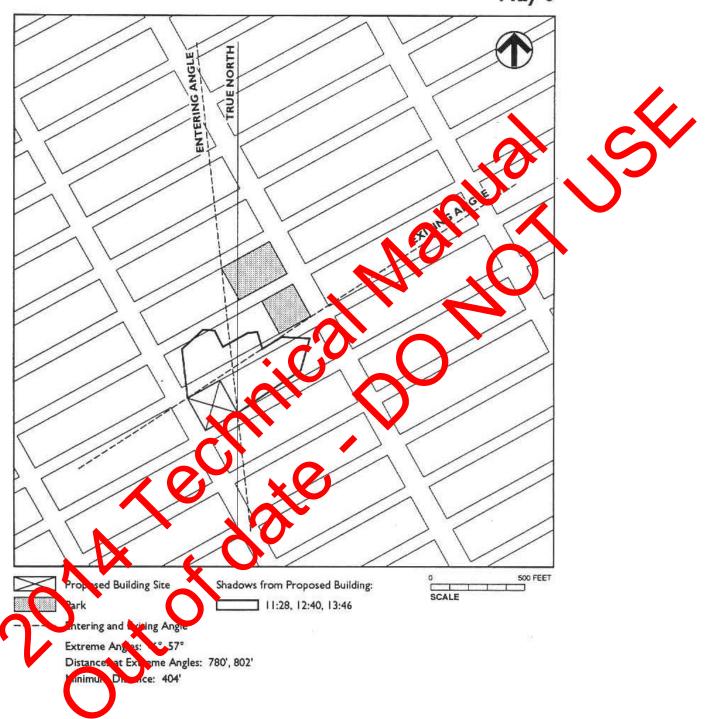




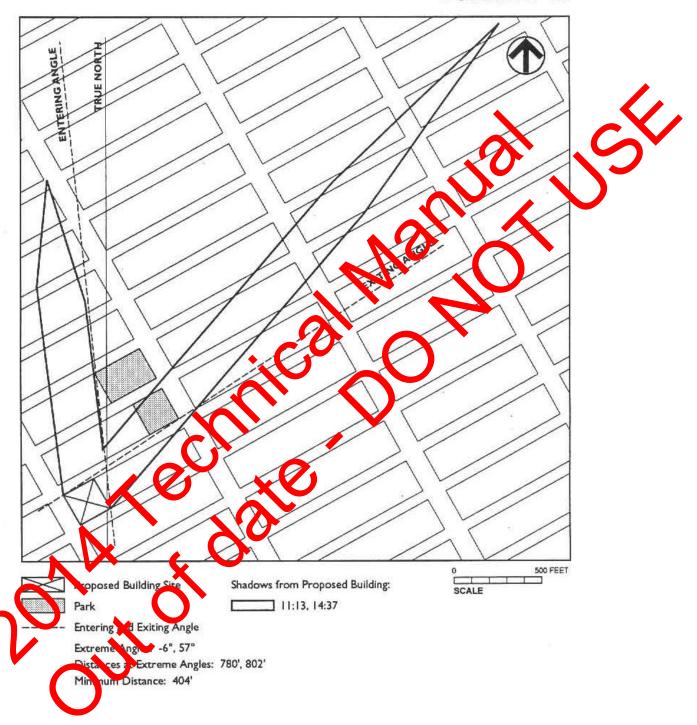
FIGURE B3

Shadows from 850-foot Building: March 21



FIGURE B4

Shadows from 850-foot Building: December 21



The length of time that the project shadows stay on the open space or resource depends on the entering and exiting angles from true north and the time of year. Because of differences in the sun's height in the sky throughout the year, shadows are longer but move more quickly (are of shorter duration) during the winter than during the summer. Using Table A2, it is possible to estimate shadow duration for each of the analysis months. For example, on March 21, the entering angle of -6 degrees would occur at approximately 11:47 a.m., and the exiting angle of 57 degrees would occur at approximately 3:04 p.m. (shown as 15:04 on the table). Thus, for a building tall enough that its shadow reaches an open space at both the entering and exiting angles, the shadow would be on some part of the park for 3 hours and 17 minutes.

If the shadow does not reach the open space or resource at both the entering and exiting angles, then the duration would be less. Using Table A2, it is possible to identify the angle (and thus the time) when the shadow would be long enough to reach and enter the park. In the March 21 example on Figure B3, because of the shape of the hypothetical building's top (it comes to a point), the shadow would not enter the park at the -6 degree angle. A line trawn rom the center of the project site (the location of the top of the roof) to the westerly point of the park yields in angle of 3 degrees. Thus, the shadow would enter the park at 12:10 p.m. EST and exit at 3:04 p.m EST for a degree and 54 minutes.

An exception to the above analysis occurs if the entering and exiting a gles are greater than 42 degrees; then, no shadows from the project would exist on December 21 for areas beyond 47 degrees. Since the sun rises and sets in the narrowest arc on that day, during the period from an hour and a half after sunrise to an hour and a half before sunset, the shadows lie between -42 and +42 degrees from true north free table A2). In this case, pick the date closest to December 21 in which at least one of the entering or exiting angles occurs, and trees winter conditions on that date. If the longest shadow for the building in question does not occur in any of the months between November and February (shadow angle more than 63 degrees), it is not necessary to consider, whater case.

To understand the shadow that would be added to an open space or natural or architectural resource by a proposed project, shadows that would exist without the project must also be defined. Other buildings may already cast shadows (or be expected to cast shadows in the future) that would eminate any new shadows cast by the proposed project. The analysis entails calculating and displaying the shadows from all buildings and structures that will be present in both the future With-Action and future Ne-Action conditions between the project site and the open space and that are also located within the two relevant entering and exiting angles from true north. The buildings in the surrounding area should also be considered for an auan circumstances: for example, extremely tall buildings farther from the open space than the project that may cast that lows within the cast fing and exiting angles (see Figure 8-8, Effects of existing buildings).

The analysis is staightforward and requires at accurate map showing the footprints of existing and proposed or planned buildings and structures. The analysis should obtain data as accurate as possible on the heights of each building and its setblets. Entering and exiting shadows are calculated and displayed for each of the representative days for analysis to the months of interest, within the timeframe window of analysis, as described in Subsections 314.3 and 314.4.

The project's shadow elect is the increment beyond shadows that would exist in the future No-Action conditions. There are, the project's shadows should be calculated and displayed clearly as an increment beyond the No-Action conditions shadows on the open space. Figures B5 and B6 illustrate a full and a partially blocked shadow from the 850-foot example building.

Once the shadow affecting the sunlight-sensitive resources have been calculated document the results as described in Section 325 and proceed with the assessment of shadow impacts as described in Section 400.



FIGURE **B5**

Incremental Shadows from 850-Foot Building: Example I

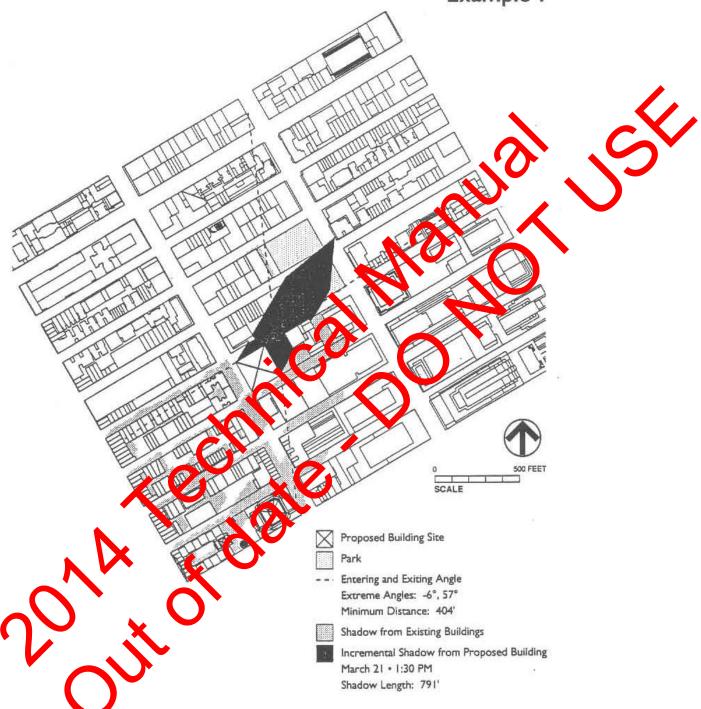




FIGURE **B6**

Incremental Shadows from 850-Foot Building: Example 2

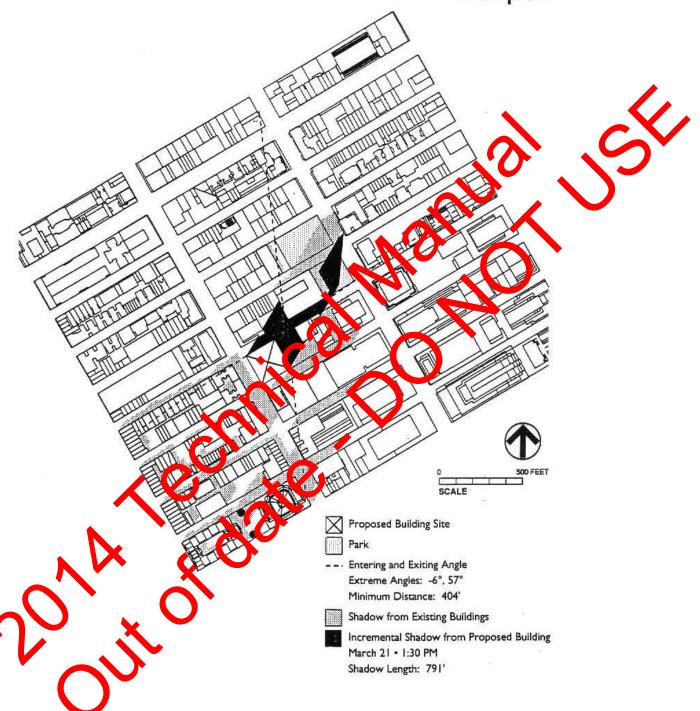




TABLE A1 - MAXIMUM SHADOW LENGTH FACTOR FOR EACH ANGLE FROM TRUE NORTH

Angle	Shadow Length	Dates	Time	Time			
	Factor*		(Eastern Standard Ti	me)			
0	2.07	12/21	11:53				
1	2.07	12/21	11:49	11:56			
2	2.07	12/21	11:45	12:00			
3	2.07	12/21	11:41	12:04			
4	2.07	12/21	11:37	12:08			
5	2.08	12/21	11:33	12:12			
6	2.09	12/21	11:29	12:16			
7	2.09	12/21	11:25	12:20			
8	2.10	12/21	11:21	12:24			
9	2.11	12/21	11:17	12.24			
10	2.13	12/21		1228			
		12/21	11:13				
11	2.14		11:09	2:36			
12	2.15	12/21	11:05	12: 1			
13	2.17	12/21	1177	12 .4			
14	2.19	12/21	10.77	12:48			
15	2.21	12/21)·53	12:52			
16	2.23	12/21	10 49	12:56			
17	2.25	12/21	10:45	13:00			
18	2.28	12/2.	10:41	13:04			
19	2.30	12/21	10:37	13:08			
20	2.34	12/21	10:31	13:13			
21	2.37	12/21	10:28	13:17			
22	2.40	1,721	20:24	13:21			
23	2.44	12/21	10. 2	13:25			
24	2.48	12/21	10 15	13:30			
25	2.52	12/21	10:11	13:34			
26	2.57	12/21	10:07	13:38			
27	2.6.	12/21	10:02	13:43			
28	2.67	12/21	9:58	13:47			
29	1.73	12/21	9:54	13:51			
30	2. 2	12/21	9:49	13:56			
31	4.						
	2 86	12/21	9:45	14:00			
32	2.93	12/21	9:40	14:05			
33	3.02	12/21	9:35	14:10			
34	3.10	12/21	9:31	14:14			
35	3.20	12/21	9:26	14:19			
36	3.31	12/21	9:21	14:24			
37	44	12/21	9:16	14:29			
38	3.5	12/21	9:12	14:33			
39	3 69	12/21	9:07	14:38			
40	3.85	12/21	9:02	14:43			
41	4.02	12/21	8:57	14:48			
42	4.27	12/20	8:51	14:55			
	•	12/21	8:51	14:55			
		12/22	8:52	14:56			
		12/23	8:53	14:57			
		12/24	8:53	14:57			
		12/25	8:54	14:58			
43	4.27	12/29	8:54	15:00			
		1/4	8:55	15:07			
44	4.19	12/7	8:41	14:53			
		1/7	8:56	15:08			
45	4.19	12/2	8:35	14:55			
		1/12	8:54	15:14			
		11/26		14:57			



		1/18	8:52	15:20
47	4.04	11/24	8:28	14:58
		1/22	8:50	15:26
48	3.99	11/20	8:24	15:00
<u> </u>		1/23	8:50	15:26
49	3.96	11/17	8:19	15:03
Ì		1/27	8:47	15:31
50	3.92	11/13	8:14	15:06
Ì		1/30	8:43	15:35
51	3.84	11/11	8:13	15:07
Ì		2/1	8:43	15:37
52	3.84	11/8	8:08	15:12
		2/3	8:40	15:40
53	3.77	11/7	8:08	11 12
		2/6	8:38	15:42
54	3.78	11/4	8:04	1.16
		2/8	8:34	15:46
55	3.72	11/1	8:00	15.20
		2/12	8:3	15:50
56	3.66	10/30	7. 9	15:21
		2/13	8:79	15:51
57	3.65	10/28	7:56	15:24
		2/15	8:26	15:54
58	3.62	10/25	7:52	15:28
		1/18	8:22	15:58
59	3.57	10/21	7:51	15:29
		2.19	22	15:58
60	3.59	10/22	7:4	15:33
		2/21	8:13	16:02
61	3.55	10/1	7:45	15:37
		2/24	8:13	16:05
62	3.40	10/18	7:45	15:37
		2/25	8:13	16:05
63	7.50	1/16	7:42	15:42
		2/28	8:09	16:07
64	3.47	10/14	7:40	15:44
		3/1	8:06	16:10
65	3.44	10/11	7:37	15:49
		3/4	8:02	16:14
66	3.40	10/10	7:36	15:50
		3/5	8:01	16:13
67	241	10/8	7:34	15:54
		3/7	7:57	16:17
				15:58
	39	10/5	/:30	
	39	10/5 3/10	7:30 7:52	16:20
)		3/10	7:52	16:20 16:00
S X	3.36	3/10 10/4	7:52 7:38	16:00
70	3.36	3/10 10/4 3/11	7:52 7:38 7:51	16:00 16:21
70		3/10 10/4 3/11 10/2	7:52 7:38 7:51 7:27	16:00 16:21 16:03
	3.36	3/10 10/4 3/11 10/2 3/13	7:52 7:38 7:51 7:27 7:48	16:00 16:21 16:03 16:24
70 71	3.36	3/10 10/4 3/11 10/2 3/13 10/1	7:52 7:38 7:51 7:27 7:48 7:27	16:00 16:21 16:03 16:24 16:05
71	3.36 3.36 3.34	3/10 10/4 3/11 10/2 3/13 10/1 3/14	7:52 7:38 7:51 7:27 7:48 7:27 7:46	16:00 16:21 16:03 16:24 16:05 16:24
	3.36	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24	16:00 16:21 16:03 16:24 16:05 16:24 16:08
71 72	3.36 3.36 3.34 3.34	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29 3/16	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24 7:43	16:00 16:21 16:03 16:24 16:05 16:24 16:08 16:27
71	3.36 3.36 3.34	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29 3/16 9/26	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24 7:43 7:21	16:00 16:21 16:03 16:24 16:05 16:24 16:08 16:27 16:13
71 72 73	3.36 3.36 3.34 3.34 3.32	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29 3/16 9/26 3/19	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24 7:43 7:21 7:39	16:00 16:21 16:03 16:24 16:05 16:24 16:08 16:27 16:13 16:31
71 72	3.36 3.36 3.34 3.34	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29 3/16 9/26 3/19 9/25	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24 7:43 7:21 7:39 7:21	16:00 16:21 16:03 16:24 16:05 16:24 16:08 16:27 16:13 16:31
71 72 73	3.36 3.36 3.34 3.34 3.32	3/10 10/4 3/11 10/2 3/13 10/1 3/14 9/29 3/16 9/26 3/19	7:52 7:38 7:51 7:27 7:48 7:27 7:46 7:24 7:43 7:21 7:39	16:00 16:21 16:03 16:24 16:05 16:24 16:08 16:27 16:13 16:31



76	3.32	9/22	7:17	16:21
		3/23	7:31	16:35
77	3.31	9/19	7:14	16:26
		3/26	7:25	16:37
78	3.24	9/17	7:14	16:28
		3/28	7:24	16:38
79	3.30	9/16	7:11	16:31
		3/29	7:21	16:41
80	3.29	9/13	7:08	16:36
		4/1	7:16	16:44
81	3.24	9/12	7:08	16:36
		4/2	7:16	16:44
82	3.29	9/10	7:05	16:4
		4/4	7:11	1(47
83	3.23	9/8	7:05	16:43
		4/6	7:10	1 48
84	3.29	9/7	7:02	16:45
		4/7	7:05	16.50
85	3.30	9/4	6:5.	16:51
		4/10		16:53
86	3.24	9/2	6:'9	16:53
		4/12	7:00	16:54
87	3.31	9/1	6:56	16:56
		4/13	6:57	16:57
88	3.29	8,30	6:55	16:59
		1/13	6:54	16:58
89	3.31	8 27	52	17:04
		4/18	6:4	17:01
90	3.29	8/25	6:51	17:05
		4/19	b:48	17:02
91	3.33	8/24	6:48	17:08
		4/21	6:45	17:05
92	3.35	8/21	6:45	17:13
		424	6:40	17:08
93	3 30	8/19	6:45	17:15
		4/26	6:39	17:09
94	3 37	8/17	6:42	17:18
•		4/27	6:36	17:12
95	3.37	8/14	6:39	17:23
		3/1	6:31	17:15
96	3.33	8/12	6:38	17:24
V		5/3	6:30	17:16
97	3.10	8/9	6:35	17:29
		5/4	6:27	17:19
98	3.42	8/6	6:31	17:33
		5/8	6:22	17:22
99	3.42	8/5	6:30	17:34
		5/10	6:20	17:24
100	3.43	8/2	6:29	17:35
		5/14	6:16	17:28
101	3.42	7/30	6:25	17:39
		5/16	6:15	17:29
102	3.48	7/28	6:22	17:42
		5/18	6:12	17:32
103	3.52	7/24	6:18	17:46
		5/22	6:09	17:37
104	3.56	7/19	6:14	17:50
		5/27	6:05	17:41
105	3.53	7/18	6:14	17:50

		5/28	6:05	17:41
106	3.59	7/13	6:10	17:54
		6/2	6:02	17:46
107	3.63	7/5	6:04	17:56
		6/10	5:59	17:51
108	3.61	6/16	6:00	17:54

Note: Negative angles and positive angles of the same value would have similar shadow length factors.

All values are for New York City, City Hall: Latitude: 40°42'23" north (40.706389°) Longitude: 74°0'29" west (74.008056°)

All times are Eastern Standard Time. Daylight Savings Time is NOT considered.

* Factor for shadow angle by degree (azimuth) from true north (0°).



TABLE A2 - SHADOW FACTORS AND TIME OF DAY FOR EACH SHADOW ANGLE, JUNE 21, MAY 6, MARCH 21, DECEMBER 21

	21 Jui	21 June		6 May ^a		21 March ^a		21 December	
Angle	Shadow Length Factor ^b	Eastern Standard Time	Shadow Length Factor ^b	Eastern Standard Time	Shadow Length Factor ^b	Eastern	Shadow Length Factor ^b	Eastern Standard Time	
-108	3.66	5:57		Time		Time		illie	
-107	3.37	6:04							
-106	3.12	6:11							
-105	2.90	6:17							
-103	2.71	6:24							
-104	2.54	6:31							
-103	2.38	6:38							
-102	2.24	6:45							
-100	2.24	6:51				1			
-99	2.00	6:58							
-98	1.89	7:05							
-98 -97	1.89	7:11	3.31	6:27			K -		
-96	1.71	7:11	3.07	6:33		-			
-95 -95	1.63	7:25	2.87	6:40	N.O.				
-93 -94	1.55	7:31	2.68	6:46					
-94 -93	1.48	7:38	2.52	6:52		1			
-93 -92	1.42	7:44	2.38	6:59					
-92 -91	1.36	7:51	2.38						
-91 -90		7:51	1	7.05					
-90 -89	1.30	8:03	2.13	71.7					
-89 -88	1.25		2.02	7.1.7 7:23					
-87	1.20 1.15	8:09 8:15	1.92	7:23					
-87 -86	1.11	8:20	1.84	7:29					
-85	1.07	8:26	68	7:41	V				
-84	1.03	8:32	1.6	7:46					
-83	0.99		1.6. 2.54						
-83 -82	0.96	8:37 8: 2	1.48) 52 1:53					
-82 -81	0.98	8:47	1.43	8:03					
-81 -80	0.90		1.43	8:09					
-79	0.87	8:53 8:57	127	8:14					
-79 -78			20	8:19					
-78 -77	0.84	9:02	1.24	8:24					
-77 -76	0.75	9:12	1.20	8:29					
-75	0.75	9: 6	1.16	8:34					
-73 -7).75	9:20	1.12	8:39	3.24	7:36			
-73 -73	0.73	9:25	1.09	8:44	3.05	7:41			
-72	0.73	9:29	1.05	8:48	2.88	7:41			
-72 -71		9:33	1.03	8:53	2.73	7:52			
-71 -70	0.67	9:33	1.00	8:57	2.73	7:57			
-70 -69	0.67	9:41	0.98	9:02	2.39	8:03			
-68	0.64	9:44	0.98	9:02	2.47	8:08			
-67	0.62	9:48	0.93	9:10	2.26	8:13			
-66	0.62	9:51	0.93	9:14	2.20	8:18			
-65	0.59	9:55	0.90	9:14	2.09	8:23			
-64	0.58	9:58	0.86	9:22	2.09	8:28			
-64 -63	0.57	10:01	0.84	9:26	1.94	8:33			
-62	0.55	10:01	0.82	9:30	1.88	8:38			
-02	0.55	10.04	0.02	ا5.50	1.00	0.30			



	21 June		6 May ^a		21 March ^a		21 December	
Angle	Shadow Length Factor ^b	Eastern Standard						
C4		Time		Time		Time		Time
-61	0.54	10:07	0.81	9:33	1.82	8:42		
-60	0.53	10:10	0.79	9:37	1.76	8:47		
-59	0.52	10:13	0.77	9:40	1.71	8:52		
-58	0.51	10:16	0.76	9:44	1.66	8:56		
-57	0.50	10:19	0.74	9:47	1.61	9:01		
-56	0.49	10:21	0.73	9:50	1.57	9:05		
-55	0.48	10:24	0.72	9:54	1.53	9:09		
-54	0.48	10:27	0.70	9:57	1.49	9:14		
-53	0.47	10:29	0.69	10:00	1.46	9:18		
-52	0.46	10:31	0.68	10:03	1.42	9.22		
-51	0.45	10:34	0.67	10:06	1.39	26		
-50	0.45	10:36	0.66	10:09	1.36	7.30		
-49	0.44	10:38	0.65	10:11	1.34	9:34		
-48	0.43	10:41	0.64	10:14	111	9:38		
-47	0.43	10:43	0.63	10:17	1.23	9:42		
-46	0.42	10:45	0.62	10:20	1 26	9·45		
-45	0.41	10:47	0.61	10:22	_ 24	9:41		
-44	0.41	10:49	0.60	10:25	1.22	۵.5		
-43	0.40	10:51	0.59	15:2	1.20	56		
-42	0.40	10:53	0.59	10 30	1.18	10:00	4.27	8:51
-41	0.40	10:55	0.58	10:32	1.16	10:03	4.02	8:57
-40	0.39	10:57	0.57	20:35		10:07	3.85	9:02
-39	0.38	10:59	0.57	10:37	1.13	10:10	3.69	9:07
-38	0.38	11:00	0.50	10:40	11	10:14	3.55	9:12
-37	0.38	11:02	55	10:42	1.10	10:17	3.42	9:16
-36	0.37	11:04	0.5	10:44	1.08	10:20	3.30	9:21
-35	0.37	11:06	0.54	1 2:46	1.07	10:24	3.20	9:26
-34	0.37	11 07	0.54	10 19	1.06	10:27	3.10	9:31
-33	0.36	11:05	0.53	10:51	1.04	10:30	3.01	9:35
-32	0.36	1:11	0.53	10:53	1.03	10:33	2.93	9:40
-31	0.35	11:12	0-	10:55	1.02	10:36	2.86	9:45
-30	0.35	11:14	52	10:57	1.01	10:39	2.79	9:49
-29	35	11:15	0.51	10:59	1.00	10:42	2.73	9:54
-28	0.33	11:17	0.51	11:01	0.99	10:45	2.67	9:58
-27	0.34	11 19	0.51	11:03	0.98	10:48	2.62	10:02
	.34	11.2	0.50	11:05	0.97	10:51	2.57	10:07
-2 <i>c</i>	0.34	11:22	0.50	11:07	0.96	10:54	2.52	10:11
-24	0.34	11:23	0.50	11:09	0.96	10:57	2.48	10:15
-23	0.54	11:25	0.49	11:11	0.95	11:00	2.44	10:22
-22	0.33	11:26	0.49	11:13	0.94	11:03	2.40	10:24
-22 -21	33	11:27	0.49	11:15	0.94	11:06	2.37	10:24
-21 -20	0.33	11:29	0.49	11:17	0.93	11:09	2.33	10:32
-20 -19	0.33	11:30	0.48	11:19	0.92	11:11	2.30	10:37
-19 -18	0.32	11:32	0.48	11:21	0.92	11:14	2.28	10:41
-16 -17	0.32	11:33	0.48	11:22	0.91	11:14	2.25	10:41
-17 -16	0.32	11:34	0.48	11:24	0.91	11:20	2.23	10:45
-16 -15	0.32	11:34	0.47	11:24	0.91	11:20	2.23	10:49
-15 -14	0.32	11:36	0.47	11:26	0.90	11:23	2.21	10:53



21 June		ne	6 May ^a		21 Mar	ch ^a	21 December	
	Shadow Length	Eastern	Shadow Length	Eastern	Shadow Length	Eastern	Shadow Length	Eastern
Angle	Factor ^b	Standard	Factor ^b	Standard	Factor ^b	Standard	Factor ^b	Standard
		Time		Time		Time		Time
-13	0.32	11:38	0.47	11:30	0.90	11:28	2.17	11:01
-12	0.32	11:40	0.47	11:31	0.89	11:31	2.15	11:05
-11	0.32	11:41	0.47	11:33	0.89	11:33	2.14	11:09
-10	0.32	11:42	0.46	11:35	0.89	11:36	2.13	11:13
-9	0.31	11:44	0.46	11:37	0.88	11:39	2.11	11:17
-8	0.31	11:45	0.46	11:39	0.88	11:41	2.10	11:21
-7	0.31	11:46	0.46	11:40	0.88	11:44	2.09	11:2.
-6	0.31	11:48	0.46	11:42	0.88	11:47		11:29
-5	0.31	11:49	0.46	11:44	0.88	11:49	7.08	1.33
-4	0.31	11:50	0.46	11:46	0.88	11:32	2.07	1
-3	0.31	11:52	0.46	11:47	0.87	1:55	2.07	11:41
-2	0.31	11:53	0.46	11:49	0.87	1:57	2.07	11:45
-1	0.31	11:54	0.46	11:51	0.87	12:00	Z 77	11:49
0	0.31	11:56	0.46	11:53	0.07	12:03	2.07	11:53
1	0.31	11:57	0.46	11:54	0.87	12:0	. 07	11:56
2	0.31	11:58	0.46	11:56	2.87	12:0	2 07	12:00
3	0.31	11:59	0.46	11:58	87	12. 0	2.07	12:04
4	0.31	12:01	0.46	11:59	0.88	12	2.07	12:08
5	0.31	12:02	0.46	12:0	0.88	2:16	2.08	12:12
6	0.31	12:03	0.46	12 /3	0.88	12:18	2.09	12:16
7	0.31	12:05	0.46	11:05	0.88	12:21	2.09	12:20
8	0.31	12:06	0.46	22:06	o.c°	12:24	2.10	12:24
9	0.31	12:07	0.46	12:08	0.88	12:27	2.11	12:28
10	0.32	12:09	0.46	12:10	189	12:29	2.13	12:32
11	0.32	12:10	47	12:12	0.89	12:32	2.14	12:36
12	0.32	12:11	0.47	12:14	0.89	12:34	2.15	12:41
13	0.32	12:12	0.47	2:15	0.90	12:37	2.17	12:44
14	0.32	12 1/	0.47	12 17	0.90	12:40	2.19	12:48
15	0.32	12:13	0.47	12:19	0.90	12:42	2.21	12:52
16	0.32	2:17	0.48	12:21	0.91	12:45	2.23	12:56
17	0.32	12:18		12:23	0.91	12:48	2.25	13:00
18	0.32	12:19	48	12:24	0.92	12:51	2.28	13:04
19	33	12:21	0.48	12:26	0.93	12:54	2.30	13:08
20	0.33	12:22	0.48	12:28	0.93	12:57	2.34	13:13
21	0.33	17 24	0.49	12:30	0.94	12:59	2.37	13:17
	.33	12:25	0.49	12:32	0.94	13:02	2.40	13:21
22	0.33	12:26	0.49	12:34	0.95	13:05	2.43	13:25
24	0.34	12:28	0.50	12:36	0.96	13:08	2.49	13:30
25	0.54	12:29	0.50	12:38	0.97	13:11	2.52	13:34
26	0.34	12:31	0.50	12:40	0.97	13:14	2.56	13:38
27	34	12:32	0.51	12:42	0.98	13:17	2.62	13:43
28	0.35	12:34	0.51	12:44	0.99	13:20	2.67	13:47
29	0.35	12:36	0.51	12:46	1.00	13:23	2.71	13:51
30	0.35	12:37	0.52	12:48	1.01	13:26	2.79	13:56
31	0.36	12:39	0.52	12:50	1.02	13:29	2.84	14:00
32	0.36	12:40	0.53	12:52	1.03	13:32	2.93	14:05
33	0.36	12:42	0.53	12:54	1.04	13:35	3.02	14:10
	5.50	1	5.55		±.5-	-5.55	5.52	± 7.10



21 June		6 May ^a		21 March ^a		21 December		
	Shadow Length	Eastern	Shadow Length	Eastern	Shadow Length	Eastern	Shadow Length	Eastern
Angle	Factor ^b	Standard	Factor ^b	Standard	Factor ^b	Standard	Factor ^b	Standard
	ractor	Time		Time	ractoi	Time		Time
35	0.37	12:45	0.54	12:59	1.06	13:41	3.20	14:19
36	0.37	12:47	0.55	13:01	1.08	13:45	3.31	14:24
37	0.38	12:49	0.55	13:03	1.10	13:48	3.44	14:29
38	0.38	12:51	0.56	13:05	1.11	13:51	3.52	14:33
39	0.38	12:52	0.57	13:08	1.13	13:55	3.67	14:38
40	0.39	12:54	0.57	13:10	1.14	13:58	3.83	14:42
41	0.39	12:56	0.58	13:13	1.16	14:02	4.00	14:40
42	0.40	12:58	0.59	13:15	1.18	14:05	- 19	14:53
43	0.40	13:00	0.60	13:18	1.20	14:09		
44	0.41	13:02	0.60	13:20	1.21	14:09		
45	0.41	13:04	0.61	13:23	1.24	1 1:15		
46	0.42	13:06	0.62	13:25	1.26	4:20		
47	0.42	13:08	0.63	13:28	1.28	14:23		
48	0.43	13:10	0.64	13:31	1.11	14:27		
49	0.44	13:13	0.65	13:34	1.33	14:37		
50	0.45	13:15	0.66	13:36	36	14:3.		
51	0.45	13:17	0.67	13:39	₋ 39	14. 9		
52	0.46	13:20	0.68	13:42	1.42	17		
53	0.47	13:22	0.69	17:4	1.45	1:47		
54	0.47	13:24	0.70	13 48	1.49	14:51		
55	0.48	13:27	0.71	1118	1.54	14:56		
56	0.50	13:30	0.73	23:55	4107	15:00		
57	0.50	13:32	0.74	13:58	1.61	15:04		
58	0.51	13:35	0.70	14:01	66	15:09		
59	0.52	13:38	78	14:05	1.70	15:13		
60	0.53	13:41	0.7	14:08	1.76	15:18		
61	0.55	13:44	81	1 :12	1.83	15:23		
62	0.56	13 47	0.82	14 15	1.87	15:27		
63	0.57	13:50	0.84	14:19	1.94	15:32		
64	0.58	3:53	0.86	14:23	2.02	15:37		
65	0.59	13:56	0.5	14:27	2.09	15:42		
66	0.61	14:00	91	14:31	2.18	15:47		
67	62	14:03	0.95	14:35	2.27	15:52		
68	0.6-	14:07	0.95	14:39	2.36	15:57		
69	0.66	14 11	0.97	14:43	2.46	16:02		
70 71	.67	14:1	1.01	14:48	2.62	16:08		
71	0.68	14:18	1.03	14:52	2.73	16:13		
72	0.70	4:22	1.06	14:57	2.86	16:18		
73	0.72	14:26	1.09	15:01	3.06	16:24		
74	0.75	14:31	1.12	15:06	3.22	16:29		
75	. 77	14:35	1.16	15:11				
76	0.79	14:39	1.20	15:16				
77	0.81	14:44	1.24	15:21				
78	0.84	14:49	1.28	15:26				
79	0.87	14:54	1.32	15:31				
80	0.89	14:58	1.37	15:36				
81	0.93	15:04	1.43	15:42				
82	0.96	15:09	1.48	15:47				



Angle	21 Jui	21 June		/ ^a	21 Mar	ch ^a	21 Dece	mber
	Shadow Length Factor ^b	Eastern Standard Time						
83	0.99	15:14	1.55	15:53				
84	1.02	15:19	1.62	15:59				
85	1.07	15:25	1.67	16:04				
86	1.11	15:31	1.75	16:11				
87	1.14	15:36	1.84	16:16				_
88	1.19	15:42	1.93	16:22				
89	1.24	15:48	2.02	16:28				
90	1.29	15:54	2.13	16:34				
91	1.36	16:01	2.24	16:40				
92	1.42	16:07	2.36	16:46		10		
93	1.48	16:13	2.54	16:53				
94	1.56	16:20	2.68	16:59				
95	1.62	16:26	2.84	17:05				
96	1.72	16:33	3.09	17:12				
97	1.79	16:39	3.29	17:18				
98	1.89	16:46						
99	2.01	16:53		•				
100	2.13	17:00						
101	2.23	17:06						
102	2.37	17:13						
103	2.54	17:20	•					
104	2.72	17:27						
105	2.92	17:34						
106	3.09	17:40						
107	3.35	17:47						
108	3.65	17:54						
109	4.00	18:01	Hall					
Notes: A	II calculations are for N	Yo C.y, ty	Hall.					

Latitude: 40°42'23" north (40.7053a

Longitude: 74°0'29" west (74.008056°)

Times are Eastern Standard times. Daylight Savings Time is NO considered. To find apparent solar time, add 4 minutes to the clock time. Then, for 21 June, no change; for 6 May, add 3 in autes; for 21 March, subtract 7 mautes, for 21 December, add 3 minutes.

Factors for May 6 and N argus 1 may be used for Augus 6 and September 21, respectively. Factor for shad, wangthr by degree (azimuth) form true north 0°.

CEQR TECHNICAL MANUAL 21 **MARCH 2014 EDITION**